Mathematics Appendix 1: Examples of formal written methods for addition, subtraction, multiplication and division

This appendix sets out some examples of formal written methods for all four operations to illustrate the range of methods that could be taught. It is not intended to be an exhaustive list, nor is it intended to show progression in formal written methods. For example, the exact position of intermediate calculations (superscript and subscript digits) will vary depending on the method and format used.

For multiplication, some pupils may include an addition symbol when adding partial products. For division, some pupils may include a subtraction symbol when subtracting multiples of the divisor.

Addition and subtraction

789 + 642 becomes	874 − 523 becomes	932 − 457 becomes	932 − 457 becomes
$$\begin{array}{r} 7\ 8\ 9 \\ +\ 6\ 4\ 2 \\ \hline 1\ 4\ 3\ 1 \\ {\scriptstyle 1\ \ 1} \end{array}$$	$$\begin{array}{r} 8\ 7\ 4 \\ -\ 5\ 2\ 3 \\ \hline 3\ 5\ 1 \end{array}$$	$$\begin{array}{r} {\scriptstyle 8\ \ 12\ 1} \\ 9\!\!\!/\ 3\!\!\!/\ 2 \\ -\ 4\ 5\ 7 \\ \hline 4\ 7\ 5 \end{array}$$	$$\begin{array}{r} {\scriptstyle 1\ \ 1} \\ 9\ 3\ 2 \\ -\ 4\!\!\!/\ 5\!\!\!/\ 7 \\ {\scriptstyle 5\ \ 6} \\ \hline 4\ 7\ 5 \end{array}$$
Answer: 1431	Answer: 351	Answer: 475	Answer: 475

Short multiplication

24 × 6 becomes	342 × 7 becomes	2741 × 6 becomes
$$\begin{array}{r} 2\ 4 \\ \times\quad 6 \\ \hline 1\ 4\ 4 \\ {\scriptstyle 2} \end{array}$$	$$\begin{array}{r} 3\ 4\ 2 \\ \times\qquad 7 \\ \hline 2\ 3\ 9\ 4 \\ {\scriptstyle 2\ \ 1} \end{array}$$	$$\begin{array}{r} 2\ 7\ 4\ 1 \\ \times\qquad\ \ 6 \\ \hline 1\ 6\ 4\ 4\ 6 \\ {\scriptstyle 4\ \ 2} \end{array}$$
Answer: 144	Answer: 2394	Answer: 16 446

Long multiplication

24 × 16 becomes	124 × 26 becomes	124 × 26 becomes

24×16 becomes

```
        2
    2   4
  × 1   6
─────────
  2 4   0
  1 4   4
─────────
  3 8   4
─────────
```

Answer: 384

124×26 becomes

```
    1   2
  1 2   4
  ×   2   6
───────────
  2 4   8   0
    7   4   4
───────────
  3 2   2   4
    1   1
```

Answer: 3224

124×26 becomes

```
    1   2
  1 2   4
  ×   2   6
───────────
    7   4   4
  2 4   8   0
───────────
  3 2   2   4
    1   1
```

Answer: 3224

Short division

$98 \div 7$ becomes

```
      1   4
    ───────
  7 | 9 ² 8
```

Answer: 14

$432 \div 5$ becomes

```
        8   6  r 2
    ───────────
  5 | 4 ³ 3   2
```

Answer: 86 remainder 2

$496 \div 11$ becomes

```
          4   5  r 1
      ───────────
  1 1 | 4   9 ⁵ 6
```

Answer: $45\frac{1}{11}$

Long division

$432 \div 15$ becomes

```
            2   8  r 12
  1   5 | 4   3   2
          3   0   0
        ───────────
          1   3   2
          1   2   0
        ───────────
          1   2
```

Answer: 28 remainder 12

$432 \div 15$ becomes

```
            2   8
  1   5 | 4   3   2
          3   0   0     15×20
        ───────────
          1   3   2
          1   2   0     15×8
        ───────────
          1   2
```

$$\frac{\cancel{12}}{\cancel{15}} = \frac{4}{5}$$

Answer: $28\frac{4}{5}$

$432 \div 15$ becomes

```
            2   8 · 8
  1   5 | 4   3   2 · 0
          3   0   ↓
        ───────────
          1   3   2
          1   2   0     ↓
        ───────────
          1   2   0
          1   2   0
        ───────────
              0
```

Answer: 28·8